Research Division Federal Reserve Bank of St. Louis *Working Paper Series* 



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Working Paper 2006-013A http://research.stlouisfed.org/wp/2006/2006-013.pdf

March 2006

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## **Inflation: Do Expectations Trump the Gap?**<sup>\*</sup>

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#### March 8, 2006

*Abstract*: We measure the relative contribution of the deviation of real activity from its equilibrium (the gap), "supply shock" variables, and long-horizon inflation expectations for explaining the U.S. inflation rate in the post-war period. For alternative specifications for the inflation driving process and measures of inflation and the gap we reach a similar conclusion: the contribution of changes in long-horizon inflation expectations dominates that for the gap and supply shock variables. Put another way, variation in long-horizon inflation expectations explains the bulk of the movement in realized inflation. We also use our preferred specification for the inflation driving process to compute a history of model-based forecasts of the inflation rate. For both short and long horizons these forecasts are close to those observed from surveys.

Keywords: Inflation persistence, Inflation forecast, Phillips Curve

JEL Codes: C32, E31

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#### **1. Introduction**

The Phillips Curve is one of the most widely recognized concepts in modern macroeconomics, and is widely used as both a theoretical construct and empirical tool. At the core of the Phillips Curve is a relationship between inflation and the real activity "gap", defined as the deviation of real economic activity from its equilibrium level. The within-sample statistical support for such a relationship in U.S. data over the post-war period is well documented in a number of studies, primary among them the work of Robert Gordon over the past 20 years (Gordon, 1982, 1997, 1998). In particular, the gap is strongly statistically significant as an explanatory variable for inflation, and this significance is robust to a broad range of specifications of the Phillips Curve. More recently, a number of papers have evaluated the out-of-sample forecasting performance of the Phillips curve. Here the evidence in favor of the gap as a driver for inflation is more mixed, with some papers documenting a substantial outof-sample relationship, (e.g. Stock and Watson, 1999), while others find that inflation forecasts from a Phillips curve are not better than those from simple benchmark models such as a random walk or an autoregression (e.g. Atkeson and Ohanian, 2001; Orphanides and Van Norden, 2003). Clark and McCracken (2003) provide a thorough exploration of the in-sample vs. out-of-sample performance of the Phillips Curve.

In this paper we revisit the importance of the gap as an explanatory variable for U.S. inflation over the post-war period. However, rather than measure importance with statistical significance, we instead focus on the relative contribution of the gap and other potential inflation drivers, such as changes in long-horizon inflation expectations and "supply shock" variables, for explaining the realized inflation rate. The initial analysis uses a specification for the inflation driving process similar to that espoused by Gordon (1982, 1997, 1998). Subsequently we

investigate a specification that replaces the distributed lag on the inflation rate present in the Gordon specification with a time-varying intercept. We show that this time-varying intercept (TVI) model can be restated in terms of the forward expectation of the inflation rate and distributed lags on the gap and supply shock variables. The results from both the Gordon and TVI specifications are clear: Changes in long-horizon inflation expectations dominate the gap and supply shock variables in the determination of actual inflation.

We then turn to more detailed analysis of the TVI model-based inflation forecasts. In particular, we use the TVI specification to construct histories of both short (one-month ahead) and long (10-year ahead) inflation forecasts and compare these to survey-based inflation forecasts. The model-based forecasts are quite close to the survey measures, suggesting that the TVI model provides a good description of the evolution of expectations. Given this success, we then use the model-based measures of expected inflation to derive time series estimates of *ex ante* real interest rates at various horizons for the past 50 years.

The remainder of the paper proceeds as follows: Section 2 presents results for the Gordon-type Phillips Curve specification, while Section 3 describes the TVI model and presents results from this specification. Section 4 compares the measures of inflation expectations from the TVI model to survey-based measures and presents new estimates of *ex ante* real interest rates over the post-war period using the model-based inflation forecasts. Section 5 concludes.

#### 2. Results from the Gordon-Type Specification

#### 2.1 Model specification and estimation

We begin with the specification that is featured in various analyses constructed by Robert Gordon:

$$\pi_t = a(L)\pi_{t-1} + b(L)D_t + c(L)X_t + \varepsilon_t \tag{1}$$

This model relates the rate of inflation to a long (typically 24 quarter) distributed lag on inflation, a distributed lag on either the unemployment rate or the deviation of the unemployment rate from a time-varying NAIRU (an index of excess demand,  $D_t$ ,) distributed lags on various supply shock variables including changes in relative import prices, changes in the relative price of food and energy, and/or deviations of productivity from trend, and dummy variables for the beginning and termination of the Nixon price controls in the early 1970s (a vector of supply shocks,  $X_t$ ). The distributed lag on inflation,  $a(L)\pi_{t-1}$ , is generally interpreted as "reflecting the influence of several past years of inflation behavior on current price-setting, through some combination of expectation formation and overlapping wage and price contracts." (Gordon, 1998, p. 303)

Our specification differs from that in Gordon (1998) in that 1) it measures the gap using the "output gap", defined as the percentage deviation of real GDP from potential GDP as measured by the CBO, 2) it uses four lags on all variables (in contrast to the 24 lags on inflation used by Gordon), and 3) it does not include the productivity deviations present in the Gordon specification. We use changes in import prices relative to the GDP price index and changes in the "core" PCE price index relative to the PCE price index as does Gordon. All the estimations follow Gordon and exclude a constant term.<sup>1</sup> We construct parallel analyses for the CPI, the PCE price index and the GDP price index, each of which is measured in quarterly percentage changes at annual rates. Our estimates over the same 1962:Q1 – 1998:Q2 sample period used in Gordon (1998) are shown in Table 1. The distributed lag variables are specified so that the

<sup>&</sup>lt;sup>1</sup> Some initial regressions were constructed that included the constant term. The estimated constant was insignificant and the estimates of the parameters of interest were unaffected by its omission.

estimated sum of the lag coefficients appears in bold as the coefficient on the first variable (the first variable in each lag distribution is in levels, all subsequent variables are first differences).

In each of the three regressions the sum of the estimated coefficients on lagged inflation is not significantly different from unity and indeed never differs from 1.0 by more than 0.01. The estimated sum of the coefficients on the output gap ranges from 0.12 to 0.18 and, consistent with prior research, is highly significant for all three price indices. The estimated sum of the coefficients on changes in relative import prices ranges from 0.2 to 0.25 and is significant in two of the three equations. The sign of the sum of the estimated coefficients on changes in the relative price of food and energy is not consistent across the three equations, and is not significant in any equation, though the impact effect of this variable is always large and significant.

#### 2.2 Stability

We investigate the robustness of these results in Figures 1-3. We construct forward and backward recursive regressions for each of the three measures of inflation. In the forward recursions the sample period always begins in 1962:Q1. Initially the sample ends in 1970:Q1 and then is extended one quarter at a time through 2005:Q1. The graphs show the sum of the lag coefficients on each of the four regressors. Once the sample gets sufficiently long, around 80 quarters, the long-run coefficients on each of the variables settles down. However, for sample periods of less than 80 quarters the estimated long-run coefficients on the output gap, changes in relative import prices and changes in relative food and energy prices are very sensitive to additional observations. For very short sample periods (24 to 40 quarters) the sum of the lagged inflation coefficients in the CPI regression is substantially less than 1.0, but as the sample length

is increased the estimate becomes very stable at close to 1.0. For the PCE and GDP measures of inflation the sum of the lagged inflation coefficients becomes close to 1.0 even for very short samples. In some cases the sum of these estimated coefficients even exceeds 1.0 implying, on the face of it, an explosive process.

In the backward recursive regressions the sample size increases from the most recent observations. In all cases the end of the sample is fixed at 2005:Q1 and the beginning of the sample is initially 1994:Q3 and then shifted backward a quarter at a time until 1962:Q1. In these experiments the estimated coefficients on the change in relative import prices and the change in the relative price of food and energy are highly unstable across sample periods that use only the data from the late 80s and 90s, regardless of the measure of inflation chosen. Over these same sample periods the estimated coefficient on the sum of the output gap terms is very small relative to the estimated value in the longer sample periods. Finally the sum of the estimated lag coefficients on inflation is very close to 1.0 regardless of the length of the sample period when the observations from the later years are always included in the regressions. In short, the inflation process in the most recent years appears to have both a permanent and a transitory component.

#### 2.3 How much does the gap contribute to explaining the inflation process?

In this subsection we investigate the relative contribution of the output gap for explaining inflation dynamics. We begin this analysis with Figure 4. The panels in this figure illustrate the "marginal adjusted  $R^{2}$ " defined as:

$$1.0 - \frac{s_{withgap}^2}{s_{nogap}^2}$$

where  $s_{withgap}^2$  is the squared standard error of estimate from the regression with all the regressors including the distributed lag on the output gap and  $s_{nogap}^2$  is the squared standard error of estimate from the regression that excludes the distributed lag on the output gap. For short sample periods, probably not surprisingly given the instability of the coefficient estimates noted above, this statistic is quite variable for the forward recursive regressions for the three measures of inflation. For the PCE and GDP measures of inflation for some samples the statistic is even negative, indicating that the other regressors account for a higher percentage of the variance of inflation in the absence of the gap terms than does the full regression specification including the gap terms. For the longer sample regressions using the PCE or GDP measures of inflation, the marginal contribution of the gap terms to accounting for the variance of inflation is quite low; on the order of 8 to 10 percent.

For the CPI measure of inflation the picture is different. The highest marginal contribution of the gap terms occurs for the shorter sample periods (late 60s and 70s) where at times the statistic exceeds 0.30. For the longer samples the statistic is generally around 0.14, substantially larger than computed for the other two measures of inflation but still indicating relatively little marginal explanatory power for the output gap terms.

The marginal adjusted  $R^2$  from the reverse recursive regressions present a contrast to the statistics for the forward recursive regressions, but do not alter the conclusion that the marginal explanatory power of the output gap terms is minimal. The results for the CPI and GDP measures of inflation are highly variable as the sample size changes. In contrast, the results for the PCE measure of inflation are negative for the samples that involve only the most recent years of data.

Another way to address this question is to compare the values of the terms  $a(L)\pi_{t-1}$ ,

 $b(L)D_t$ ,  $c(L)X_t$  and  $\varepsilon_t$  for a regression over the entire sample period. These are shown in Figure 5-7 for regressions constructed on the sample 1964:2 – 2005:1. The message from these graphs is apparent and consistent with the analysis above: the output gap (and supply shock variables) accounts for only a minor portion of fluctuations in inflation in this specification regardless of the measure of inflation. In summary: for this model, expectations, as proxied by a distributed lag on inflation whose coefficients sum to 1.0, trump the gap!

#### 3.1 Results from the Time-Varying Intercept Specification

Suppose that the distributed lag on inflation in the Gordon specification represents a proxy for long-horizon expected inflation that is specified to appear with a coefficient of 1.0 so that the long-run Phillips curve is vertical:

$$\pi_t = 1.0\pi_t^e + b(L)D_t + c(L)X_t + \varepsilon_t$$
(2)

Alternatively this equation can be thought of as specifying a time-varying intercept (the expected rate of inflation) on a vector of 1.0's:

$$\pi_t = 1.0z_t + b(L)D_t + c(L)X_t + \varepsilon_t \tag{3}$$

We assume that  $z_t$  follows a random walk:<sup>2</sup>

$$z_t = z_{t-1} + \mu_t \tag{4}$$

<sup>&</sup>lt;sup>2</sup> This is similar to Gordon's specification of the time-varying NAIRU in his 1997 and 1998 papers.

Equation (4) implies that, assuming stationarity of  $D_t$  and  $X_t$ , the infinite-horizon forecast of inflation is equal to  $z_t$  (see Beveridge and Nelson, 1981). Thus,  $z_t$  has the interpretation of the long-horizon inflation expectation.<sup>3</sup>

The model in (3) and (4) can be estimated via maximum likelihood using the Kalman filter. The estimates of the lag polynomials b(L) and c(L) are shown in Table 2 for the sample period 1964:Q2 to 2005:Q1. Table 3 instead reports results from an expanded specification. First, we extend the sample period to include data subsequent to the end of the Korean War. Since the core PCE data are not available before 1959, we recomputed the relative change in food and energy prices using CPI data. The "core CPI" is available starting in 1957. Prior to 1957 we use the all items CPI less food rather than the "core CPI". The two series are highly correlated in the late 1950s, since energy prices were not highly volatile until the early 1970s. Prior to 1987 we compute the relative change in food and energy prices using CPI data. We do this to avoid the truncation problems that affect the computation of CPI inflation rates in the early part of the sample period when the base year is 1982-84 = 100 (see Kozicki and Hoffman, 2004).

Second, we allow for three breaks in the variance of the innovations to the time-varying intercept process. We date the first break at 1967:Q1 representing the beginning of the Great Inflation. We date the second break at 1984:Q1 representing the beginning of the "Great Moderation" (Kim and Nelson, 1999; McConell and Perez-Quiros, 2000). We date the third break at 1994:Q1 when the FOMC started releasing information on changes in the intended

<sup>&</sup>lt;sup>3</sup> Equation (4) assumes that the shocks to long-horizon inflation expectations are frequent and continuous. An alternative is that shocks to long-horizon inflation expectations are infrequent and discrete. For an example of such a specification for modeling U.S. inflation see Levin and Piger (2002, 2006).

federal funds rate at the close of FOMC meetings. In all three specifications the estimated variance of the innovations to the time-varying intercept increases sharply during the Great Inflation, falls to 40-50 percent of its 1953-66 value during the first decade of the Great Moderation, and then declines by roughly 50 percent of the value in the 1984-93 period during the most recent decade (see Figure 18 for a plot of the estimated innovations). We interpret the latest decline as evidence that long-horizon inflation expectations have become better "anchored" during the period of increasing FOMC transparency. Note however that this is not necessarily evidence of a causal relationship between increased transparency and lower volatility of long-term inflation expectations.

The estimates of the time-varying intercept and the contributions of the gap and supply shocks from the estimates in Table 3 are shown in Figure 8 for the CPI, PCE and GDP inflation models respectively. These graphs indicate that the time-varying intercept term, which serves as our measure of long-horizon inflation expectations, dominates the variation in all three measures of inflation. The only cases where the distributed lags on the output gap and the supply shock terms account for a substantial portion of the inflation rates are in 1973-4 and to a lesser extent in 1979-80. Finally, Figure 9 demonstrates that the estimated autocorrelations of estimated residuals of the PCE and GDP inflation equations are very small, though there is some autocorrelation in the residuals of the CPI inflation equation.

In Table 4 another set of regressions with a time-varying intercept are reported, but in this case the CBO measure of the output gap has been replaced by the difference between the unemployment rate and a time-varying estimate of the NAIRU. We follow Gordon (1997) and model the NAIRU as a random walk and constrain the standard deviation of the error term in this process to 0.2. In addition a restriction on the level of the NAIRU is required in order to identify

this process in the presence of the time-varying intercept term. We have restricted the NAIRU to equal the unemployment rate in 1995:1, consistent with Figure 3 in Gordon (1997). These results are substantially the same as those obtained with the CBO output gap, suggesting that our conclusions about the contribution of the gap are not sensitive to whether it is measured as an output or unemployment gap.

#### 4. TVI Model-Based Inflation Forecasts

The TVI specification in equations (3-4) can be rewritten in terms of the forward expectation of the inflation rate and distributed lags on the gap and supply shock variables, a specification that has much in common with the "New Keynesian" formulation of the Phillips curve (Clarida, Gali and Gertler, 1999). To begin, rewrite equation (3) as:

$$\pi_{t} = z_{t} + \sum_{i=0}^{N} \alpha_{i} \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + \varepsilon_{t}$$
(5)

where  $a_i$  is a vector of coefficients taken from the lag polynomials b(L) and c(L) and N is the lag order of these lag polynomials. Incrementing the time index in equation (5) by one quarter and taking expectations yields:

$$E_{t}[\pi_{t+1}] = E_{t}[z_{t+1}] + \alpha_{0}E_{t}\begin{bmatrix}D_{t+1}\\X_{t+1}\end{bmatrix} + \sum_{i=1}^{N}\alpha_{i}\begin{bmatrix}D_{t+1-i}\\X_{t+1-i}\end{bmatrix},$$
(6)

Assume that  $\begin{bmatrix} D_{t+1} \\ X_{t+1} \end{bmatrix}$  can be modeled as a stationary VAR process:

$$\begin{bmatrix} D_{t+1} \\ X_{t+1} \end{bmatrix} = \sum_{i=0}^{J} \beta_i \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + v_{t+1}^{4}$$
(7)

Then:

$$E_{t}[\pi_{t+1}] = z_{t} + \alpha_{0} \sum_{i=0}^{J} \beta_{i} \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + \sum_{i=1}^{N} \alpha_{i} \begin{bmatrix} D_{t+1-i} \\ X_{t+1-i} \end{bmatrix}.$$
(8)

Since  $\begin{bmatrix} D_t \\ X_t \end{bmatrix}$  is assumed to be stationary,  $\lim_{M \to \infty} E_t \pi_{t+M} = z_t$ . Thus  $z_t$  represents the long horizon

inflation forecast from the model and, in the sense of Beveridge and Nelson (1981), represents the long-run or permanent component of expected inflation. Likewise,

$$\alpha_0 \sum_{i=0}^{J} \beta_i \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + \sum_{i=1}^{N} \alpha_i \begin{bmatrix} D_{t+1-i} \\ X_{t+1-i} \end{bmatrix}$$
 is then the one-period ahead transitory component of expected

inflation.<sup>5</sup>

The inflation forecast error from the TVI specification is given by:

$$\pi_{t+1} - E_t \left[ \pi_{t+1} \right] = \mu_{t+1} + \alpha_0 \left[ \begin{bmatrix} D_{t+1} \\ X_{t+1} \end{bmatrix} - \sum_{i=0}^J \beta_i \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} \right] + \varepsilon_{t+1} = \mu_{t+1} + \alpha_0 v_{t+1} + \varepsilon_{t+1}.$$
(9)

<sup>4</sup> Our forecasting model for  $\begin{bmatrix} D_{t+1} \\ S_{t+1} \end{bmatrix}$  is a restricted four lag VAR. Estimates of an unrestricted VAR,

 $\begin{bmatrix} I - \beta(L) \end{bmatrix} \begin{bmatrix} D_{t+1} \\ S_{t+1} \end{bmatrix} = v_{t+1}$  indicated a lower triangular structure for  $\beta(L)$  when the three variables are ordered 1) relative food and energy price changes, 2) relative import price changes and 3) the output gap. This structure was imposed to generate our forecasts.

<sup>5</sup> By constructing multistep dynamic forecasts of  $\begin{bmatrix} D_{t+i} \\ X_{t+i} \end{bmatrix}$  the entire path of the transitory component of expected inflation can be estimated.

Thus unexpected inflation is the sum of three terms: 1) the innovation to long-horizon inflation expectations, 2) the one-period ahead forecast error for  $\begin{bmatrix} D_{t+1} \\ X_{t+1} \end{bmatrix}$ , and 3) the residual of the

"Phillips curve." When  $\alpha_0 = 0$  the one-period ahead unexpected inflation is just

$$\pi_{t+1} - E_t[\pi_{t+1}] = \mu_{t+1} + \varepsilon_{t+1}.$$

Finally, given the expression for  $E_t[\pi_{t+1}]$ , the "Phillips Curve" can be rewritten as the sum of the forward expectation of the inflation rate and distributed lags on the gap and supply shock variables:

$$\pi_{t} = E_{t} \Big[ \pi_{t+1} \Big] - \alpha_{0} \sum_{i=0}^{J} \beta_{i} \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + \sum_{i=0}^{N-1} [\alpha_{i} - \alpha_{i+1}] \begin{bmatrix} D_{t-i} \\ X_{t-i} \end{bmatrix} + \alpha_{N} \begin{bmatrix} D_{t-N} \\ X_{t-N} \end{bmatrix} + \varepsilon_{t} \,. \tag{10}$$

In Figures 10a - 12a the actual inflation rates are plotted against the one-period ahead projections  $(E_{t-1}[\pi_t])$  using the estimated coefficients from Table 5. The middle panels of each figure (10b - 12b) show the differences in the series from the top panels – the one-period ahead inflation forecast errors.<sup>6</sup> Finally, the lower panels of each figure (10c - 12c) show the first 12 autocorrelations of the computed one-period ahead inflation forecast errors. Note that for all three inflation measures the autocorrelations are very small indicating that there is little predictive content in the history of the forecast errors for future forecast errors.

In Figure 13 we compare our estimates of the one-period ahead inflation rate with various survey measures of inflation. There are two surveys that are available for CPI inflation: a onequarter ahead inflation forecast from the Survey of Professional Forecasters (available from

<sup>&</sup>lt;sup>6</sup> For purposes of these graphs, we incorporate the effects of the Nixon price control dummy variables, Nixon\_On and Nixon\_Off. While these variables were constructed by Gordon *expost*, we believe it is reasonable to assume that at the time individuals expected some impact on inflation in the short run of the implementation and removal of the controls.

1981:3 through 2005:1) and a one-quarter ahead inflation forecast from the Blue Chip (available from 1985:1 through 2005:1). The inflation expectation measure from the TVI model is plotted in black in all three panels of Figure 13. The forecasts from the Survey of Professional Forecasters are plotted in blue (SPF 1-quarter) and the forecasts from the Blue Chip are plotted in Green (BC1-quarter). There is one survey available for GDP inflation: a one-quarter ahead forecast from the Survey of Professional Forecasters (available from 1968:4 through 2005:1). This is plotted in blue (SPF 1-quarter) in the bottom panel of Figure 13. From the early 80s, the TVI estimates track the respective survey measures quite closely. In particular for CPI inflation the major spikes in the time-varying intercept estimates of inflation are mirrored in the timing, and in many cases in the amplitude by spikes in the SPF 1-quarter measure. The Blue Chip CPI inflation forecasts are less volatile that the other two measures, but again the major spikes in this series mirror the timing of the major spikes in the series derived from the time-varying intercept model. This visual impression is confirmed by heteroskedasticity and autocorrelation consistent regressions of the inflation forecast from the TVI model  $(E_{t-1}[cpi_t])$  on the corresponding survey measure. For the sample period 1981:3 – 2005:1 the regression with the Survey of Professional Forecasters measure is:

$$E_{t-1}cpi_t = 0.06 + 1.08spf\_cpi_t + \mathcal{E}_t \qquad \overline{R}^2 = .68, \ see = 1.13, dw = 2.00$$
(0.45) (0.14)

while for the sample period 1985:1 - 2005:1 the regression with the Blue Chip measure is:

$$E_{t-1}cpi_t = 0.19 + 1.00bc_1Q_t + \varepsilon_t$$
(0.37) (0.11)  $\overline{R}^2 = .49, \ see = 0.94, dw = 2.16$ 

In both regressions the estimated constant term is not significantly different from zero and the estimated coefficient of the survey measure is not significantly different from one. The

estimated standard errors of the residuals of these regressions are fairly large, but the Durbin-Watson statistics do not indicate any first-order serial correlation.

For the GDP inflation measure we have data to compare with a survey starting in late 1968. There are substantial differences in the two measures in the late 1960s and then again in 1973. The latter period is strongly influenced by our decision to include the estimated effect of the removal of the price controls in the TVI measure of expected inflation. After 1973 the two measures track quite well, though the spikes in the time-varying coefficient measure are not as well aligned with the survey data as is the case with the CPI inflation rate. A regression of the TVI measure ( $E_{t-1}gdp_t$ ) on the survey measure over sample period 1968:4 – 2005:1 is:

$$E_{t-1}gdp_t = -0.07 + 1.09spf_gdp_t + \mathcal{E}_t$$
(0.22) (0.07)  $\overline{R}^2 = .78, see = 1.20, dw = 1.12$ 

Again the estimated constant term is not significantly different from zero nor is the estimated coefficient on the survey measure of GDP inflation significantly different from one. The estimated standard error of the residuals is comparable to that found for the CPI inflation regressions, but in this case the Durbin-Watson statistic suggests that substantial first-order serial correlation remains in the estimated residuals.

The estimated time series of the time-varying intercept (the permanent component of expected inflation) are shown in Figure 14. The series for all three inflation rates are quite similar, though the one derived from the CPI is more volatile than the other two up to the "Great Moderation" period. The yellow shaded area is drawn for reference between two and four percent. The estimates suggest that long-term expected inflation rose sharply in the late 60s from less than 2 percent in 1964 to over 4 percent in 1968. All three series level off in the late 60s and decline a bit in the early 70s before the first energy shock. From 1973 until 1982 all the series

trend up. From 1982-85 the trend is reversed and the series level out around 4 percent for the remainder of the 80s. After 1990 all the series again trend down through the mid 90s, after which they level out around 2 percent.

The final line (SPF\_10) plotted on Figure 14 is the 10-year ahead CPI inflation forecast from the Survey of Professional Forecasters. The general trend in the long-term expected CPI inflation from the TVI model tracks that in the survey data quite well for the period for which the latter series are available: 1991:4 through 2005:1. A regression of the model generated data on the survey data shows:

$$\overline{Z}_{-cpi} = -0.83 + 1.23Spf_{-inf}$$
(0.21) (0.08) 
$$\overline{R}^{2} = .86, see = 0.24, dw = 0.63$$

The constant in the regression is significantly less than zero and the coefficient on the survey data is significantly greater than one. These results are driven by the constant value of the survey data over the past five years. Nevertheless the relationship between the two series is quite close as judged by the large  $\overline{R}^2$  and the low estimated standard error of the residuals.

Goodfriend (1993) hypothesizes four periods of "inflation scares" during the 1980s. These periods are December 1979 through February 1980, June 1980 through October 1981, May 1983 through August 1983 and March 1987 through October 1987. He defines "a significant long-rate rise in the absence of an aggressive funds rate tightening an inflation scare since it reflects rising expected long-run inflation" (p.8). Hence his inflation scares are inferred from the behavior of long-term rates relative to short-term rates. Since we have a measure of long-term inflation expectations that is derived independently of any information on the behavior of interest rates, the estimates can be used as an independent check on Goodfriend's inflation scare hypothesis. The approximate periods designated as inflation scares are shaded in Figure 14.<sup>7</sup> Our measure of long-term expected CPI inflation jumps up sharply in the first three designated inflation scares. There are no sharp increases in our measures of long-term expected PCE or expected GDP inflation for the first two designated inflation scares. For the third inflation scare, the measure of expected long-term PCE inflation jumps up, but this follows a short-lived downward spike of almost the same magnitude. The measure of expected long-term GDP inflation continues on a downward trend during the third inflation scare. Finally, none of our measures of long-term expected inflation exhibit any major movement during the fourth period designated as an inflation scare. Hence from our measures of long-term expected inflation there is little supporting evidence for the inflation scare hypothesis.

As an alternative check on whether the estimated time-varying intercept is a reasonable proxy measure for long-term expected inflation, we can subtract the estimated  $z_t$  for each of the three inflation equations from a long-term rate of interest to get an estimated *ex ante* long-term real rate. We use the 10 year Treasury bond rate. These estimates are shown in Figures 15a-c. The horizontal line is drawn for reference at 2 percent. In recent history there are two comparison measures. Beginning in 1991 the Survey of Professional Forecasters reported survey responses for a 10 year-ahead CPI inflation rate. The difference between the 10 year nominal rate and these survey responses is plotted as the blue line in Figures 15a-c. Since 1997 the U.S. Treasury has issued long-term indexed bonds. The yield on these bonds is shown as the green line in Figures 15a-c.<sup>8</sup>

<sup>&</sup>lt;sup>7</sup> The shaded periods are only approximate since Goodfriend worked with monthly data and our models are estimated on quarterly data.

<sup>&</sup>lt;sup>8</sup> The comparisons are only exact in Figure 21a since the Survey of Professional Forecasters refers to the CPI and the TIPS are indexed to the CPI.

Regressions of the implied long-term real rates from the TVI model on the implied longterm real rate from the Survey of Professional Forecasters over the sample period 1991:4-2005:1 are:

$$\begin{aligned} ltrate - Zcpi &= 0.15 + 1.00 [ltrate - spf _ 10] \\ (0.12) (0.05) \\ \hline R^2 &= .90, \ see = 0.27, dw = 0.45 \\ ltrate - Zpce &= 0.55 + 1.05 [ltrate - spf _ 10] \\ (0.08) (0.04) \\ \hline R^2 &= .92, \ see = 0.24, dw = 0.40 \\ ltrate - Zgdp &= 0.51 + 1.10 [ltrate - spf _ 10] \\ (0.06) (0.02) \\ \hline R^2 &= .98, \ see = 0.13, dw = 1.05 \end{aligned}$$

Strictly speaking only the first of these three regressions is an exact comparison, since the survey data refer the CPI. In that regression the estimated constant term is not significantly different from zero, and the estimated coefficient on the survey measure of the real long-term rate is not significantly different from one. Hence the two measures appear on average to differ by an insignificant constant (with the model generated estimate larger) and to move up and down together during the sample period. The same conclusion is appropriate for the model based measure of the long-term real rate based on PCE inflation relative to the long-term real rate derived from the survey data, though in this case the average difference is significantly different from zero. The regression with the long-term real rate derived from the model based estimate of long-term GDP inflation moves significantly more than one-for-one with the real rate derived from the survey data.

A second comparison of real rates is provided by the Treasury indexed bond data, though only for a short time period: 1997:1 – 2005:1. The real long-term rates derived from our model of long-term expected inflation for all three measured inflation rates do not move significantly differently from one-for-one with the TIPS rate over this sample period.

In all three cases the estimated standard error of the residuals of the regressions are larger than the estimated standard error of the residuals from the corresponding regression with the survey based measures of the long-term real rate. This may suggest a closer relationship between our model-based estimates and the survey based estimates than between the model-based estimates and the TIPS rates, but the differences may only reflect the relatively short sample period during which the TIPS rates are available.

The model can be used to generate multiperiod inflation forecasts for any horizon. As the horizon gets longer the forecast of the transitory component of inflation goes to zero and the forecast converges on the estimated permanent component of inflation. The forecasts for inflation one to four quarters ahead can be combined to generate a one-year ahead inflation forecast. This forecast is subtracted from the one-year constant maturity Treasury rate to produce a one-year ahead estimated *ex ante* real rate. These model based one-year real rates are plotted in Figure 16a-c along with one-year real rates derived using Michigan, Survey of Professional Forecasters and Blue Chip survey measures of future CPI and GDP inflation rates. For the CPI measures, the model-based real rates track the survey-based measures very closely since the 1980s when the survey data start. The model-based measure for GDP inflation tracks the measure derived from the Survey of Professional Forecasters since the mid 1970s.

Finally, we can use the model-based estimates of one-period ahead expected inflation and a three month interest rate to construct an *ex ante* three month real rate. The nominal rate that we use for these calculations is the secondary market rate on three month Treasury bills. In Figure 17a-c we compare the term structure of real interest rates. In each panel of that figure the black line is the one-quarter ahead real rate computed from our models, the blue line is the modelbased one-year ahead real rate, and the green line is the model-based long-term (10 year) real rate discussed in the previous section. The results in the three panels are quite consistent. In each case the real term structure appears very flat throughout the 1960s. In the 1970s the real term structure became positively sloped. The really interesting period is that of the early 1980s the period of the New Operating Procedures. During this period the model based estimates imply that the real term structure shifted up rapidly, but that the term structure remained essentially flat for the entire period. There is no evidence that the estimated real term structure inverted during this period, though the nominal term structure became sharply inverted at the time. Beginning in the early 80s the real term structure is almost always positively sloped and is the steepest in 1990-2 and since 2000. In those two periods real rate spreads in the 1-10 year range became quite large, but those in the 3-month to 1-year range remained relatively small.

### 5. Conclusion

We have presented evidence regarding the relative contribution of the real activity "gap" and other potential inflation drivers, such as changes in long-horizon inflation expectations and supply shock variables, for explaining the U.S. inflation rate over the post-war period. Our results present a different picture of the inflation process than the conventional wisdom. In particular, they suggest that realized inflation is dominated by variation in long-horizon expected

inflation, while the gap and supply shock variables play only a very limited role. These results are robust to alterative specifications for the inflation driving process and measures of inflation and the gap.

Our preferred model specification is one in which inflation is determined by a random walk permanent component (which represents the long-horizon inflation expectation), a distributed lag on the real activity gap, and a distributed lag on supply shock variables. Model-based inflation forecasts align closely with forecasts obtained from surveys at all horizons during the years for which the survey data is available. This suggests that our model of the inflation driving process does a very good job of reproducing whatever process is driving survey measures of future inflation. Results from this model also suggest that the variance of the process that generates changes in long-term expected inflation has changed over time. Interestingly, this variance has become very small over the last 10 years of the sample, suggesting that long-term expected inflation has become much better "anchored" in the past decade.

Taken together, the evidence presented here suggests that the key to understanding the inflation process is to understand what drives changes in long-horizon inflation expectations. To this end, further research focused on attempting to relate these changes to "news" could prove especially fruitful.

### References

Atkeson, A. and L.E. Ohanian, 2001, "Are Phillips Curves Useful for Forecasting Inflation?," *Federal Reserve Bank of Minneapolis Quarterly Review*, 25, 2-11.

Beveridge, S. and C.R. Nelson, 1981, "A New Approach to Decomposition of Economic Time Series into Permanent and Transitory Components with Particular Attention to Measurement of the Business Cycle," *Journal of Monetary Economics* 7, 151-174

Clarida, R., J. Galí and M. Gertler (1999), "The Science of Monetary Policy: A New Keynesian Perspective," *Journal of Economic Literature*, 37, 1661-1707.

Clark, T. E. and M. W. McCracken, 2003, "The Predictive Content of the Output Gap for Inflation: Resolving In-Sample and Out-of-Sample Evidence," Federal Reserve Bank of Kansas City working paper RWP 03-06.

Goodfriend, M., 1993, "Interest Rate Policy and the Inflation Scare Problem: 1979-1992," *Federal Reserve Bank of Richmond Economic Quarterly*, 79, 1-24.

Gordon, R. J. (1982), "Inflation, Flexible Exchange Rates and the Natural Rate of Unemployment," in Baily, M.N., ed., *Workers, Jobs and Inflation*, Washington, DC: Brookings Institution, pp. 88-152.

Gordon, R. J. (1997), "The Time-Varying NAIRU and its Implications for Economic Policy," *Journal of Economic Perspectives*, 11, 11-32.

Gordon, R. J. (1998), "Foundations of the Goldilocks Economy: Supply Shocks and the Time Varying NAIRU," *Brookings Papers on Economic Activity*, 2, 297-333.

Kim, C.-J., and Nelson, C. R. (1999), "Has the U.S. Economy Become More Stable? A Bayesian Approach Based on a Markov-switching Model of the Business Cycle," *The Review of Economics and Statistics*, 81, 608-616.

Kozicki, S. and B.Hoffman, (2004), "Rounding Error: A Distorting Influence on Index Data," *Journal of Money, Credit, and Banking*, 36, 319-338.

Levin, A. and Piger, J. (2002), "Is Inflation Persistence Intrinsic In Industrial Economies?," Federal Reserve Bank of St. Louis Working Paper #2002-023.

Levin, A. and Piger, J. (2006), "Bayesian Model Selection for Multiple Structural Break Models," Federal Reserve Bank of St. Louis Working Paper #2006-???.

McConnell, M. M. and Quiros, G. P. (2000), "Output fluctuations in the United States: What has Changed Since the Early 1980s?," *American Economic Review*, 90, 1464-1476.

Orphanides, A. and S. van Norden, 2003, "The Reliability of Inflation Forecasts based on Output Gap Estimates in Real Time," Scientific Series 2003s-01, CIRANO.

Stock, J. H. and M.W. Watson (1999), "Forecasting Inflation," *Journal of Monetary Economics* 44, 293-335.

### Table 1: Gordon-Type Regressions

	CPI	PCE	GDP
$\pi_{t-1}$	1.01	1.00	0.99
	(0.02)	(0.02)	(0.02)
$\Delta \pi_{c,1}$	-0.68	-0.67	-0.58
<i>t</i> -1	(0.08)	(0.09)	(0.09)
$\Delta \pi_{c2}$	-0.71	-0.44	-0.42
- <i>I</i> -2	(0.08)	(0.10)	(0.09)
$\Lambda\pi$	-0.35	-0.27	-0.29
	(0.08)	(0.09)	(0.08)
Gap	0.18	0.12	0.13
- 11	(0.05)	(0.03)	(0.04)
∧ <i>Gap</i>	-0.03	0.07	0.05
	(0.13)	(0.08)	(0.04)
AGap.	0.18	0.01	0.00
	(0.13)	(0.08)	(0,10)
AGan .	0 15	-0.01	0.04
	(0.13)	(0.08)	(0,10)
AGan	0.04	-0.13	0.09
$\Delta Oup_{t-3}$	(0.12)	(0.08)	(0.09)
A Rel Import Prices.	(0:12) 0 24	(0.00) 0 20	0.03)
	(0.13)	(0.09)	(0.11)
$\Lambda^2$ Rel Import Prices.	-0.15	-0.06	-0.39
	(0.12)	(0.08)	(0.10)
$\Delta^2 Rel Import Prices_{t-1}$	0.00	0.08	-0.15
-	(0.11)	(0.07)	(0.09)
$\Delta^2 Rel Import Prices_{t-2}$	0.05	0.10	-0.03
2	(0.09)	(0.06)	(0.08)
$\Delta^2 Rel Import Prices_{t-3}$	0.02	0.13	0.04
A Rol Ed & Energy Prices	(0.07)	(0.05)	(0.06) -0.47
$\Delta$ Kei FU & Energy Prices <sub>t</sub>	-0.37 (1.05)	(0.71)	-0.47 (0.83)
$\Lambda^2$ Pol Ed & Energy Prices	(1:05)	2.06	(0.00)
$\Delta$ Kei Fu & Energy Frices <sub>t</sub>	4.50	0.66)	2.31
$\Lambda^2$ Pol Ed & Energy Prices	(0:50)	(0.00)	(0.70)
$\Delta$ Kei Fu & Energy Frices <sub>t-1</sub>	(0.97)	2.15	1.70 (0.74)
$\Lambda^2$ Pol Ed & Energy Prices	(0.97)	(0.09)	(0.74)
$\Delta$ Kei Fu & Energy Frices <sub>t-2</sub>	0.91	1.05	0.55
$\Lambda^2$ Pol Ed & Enormy Prices	(0.00)	(0.03)	(0.03)
$\Delta$ Kei Fa & Energy Frices <sub>t-3</sub>	2.41	0.20	0.19
NIXON ON	-1 75	-1 21	-0.99
	(0.66)	(0.46)	(0.53)
NIXON_OFF	2.84	1.09	1.55
= 2	(0.72)	(0.51)	0.58
	0.88	0.91	0.87
Mean Inflation Rate	4.63	2.59	4.13
Standard Error of the Estimate	3.16 1 1 1	2.59	2.51
Durbin-Watson Statistic	2 18	2.05	0.09 2 12
			<u></u>

## Table 2: Time-varying Intercept Regressions with CBO Gap

	CPI	PCE	GDP
Standard Deviation of Intercept	0.58 (0.07)	0.42 (0.06)	0.37 (0.05)
$Gap_t$	0.16	-0.01	-0.02
	(0.10)	(0.07)	(0.08)
$Gap_{t-1}$	0.06	0.18	0.11
	(0.12)	(0.09)	(0.10)
$Gap_{t-2}$	-0.05	-0.04	-0.03
	(0.12)	(0.09)	(0.10)
$Gap_{t-3}$	0.19	-0.07	0.04
	(0.12)	(0.09)	(0.10)
$Gap_{t-4}$	-0.01	0.15	0.06
	(0.10)	(0.07)	(0.08)
$\Delta$ Rel Import Prices <sub>t</sub>	0.11	0.12	-0.23
	(0.05)	(0.04)	(0.05)
$\Delta$ Rel Import Prices <sub>t-1</sub>	0.06 (0.06)	0.11 (0.04)	0.11 (0.05)
$\Delta$ Rel Import Prices <sub>t-2</sub>	0.10 (0.06)	0.02 (0.05)	0.02 (0.05)
$\Delta$ Rel Import Prices <sub>t-3</sub>	-0.01 (0.06)	0.07 (0.04)	0.11 (0.05)
$\Delta$ Rel Import Prices <sub>t-4</sub>	0.04 (0.05)	0.02 (0.04)	0.05 (0.04)
$\Delta$ Rel Fd & Energy Prices <sub>t</sub>	2.85	2.04 (0.21)	1.33
$\Delta$ Rel Fd & Energy Prices <sub>t-1</sub>	0.31 (0.28)	0.17 (0.21)	0.32 (0.23)
$\Delta$ Rel Fd & Energy Prices <sub>t-2</sub>	0.10 (0.29)	0.08 (0.20)	0.26 (0.23)
$\Delta$ Rel Fd & Energy Prices <sub>t-3</sub>	0.36 (0.28)	-0.21 (0.21)	0.05 (0.26)
$\Delta$ Rel Fd & Energy Prices <sub>t-4</sub>	-0.10 (0.28)	0.26 (0.20)	0.40 (0.23)
NIXON_ON	-0.84 (0.94)	-0.63 (0.69)	-1.37 (0.71)
NIXON_OFF	3.02 (0.77)	2.12 (0.56)	2.46 0.60
Log Likelihood	-329.65	-265.28	-285.09
Standard Error of the Estimate	0.83	0.61	0.74

# Table 3: Time-varying Intercept Regressions with CBO Gap and break in theVariance of the Intercept in 1967, 1984 and 1994

	CPI	PCE	GDP
Standard Deviation of Intercept 53-66	0.79	0.47	0.52
Standard Deviation of Intercept 67-83	1.92	(0.12)	0.75
	(0.19)	(0.16)	(0.21)
Standard Deviation of Intercept 84-93	0.36	0.26	0.22
	(0.09)	(0.06)	(0.08)
Standard Deviation of Intercept 94-05	(0.05)	(0.06)	(0.08)
Gap,	-0.01	-0.09	-0.10
	(0.07)	(0.07)	(0.09)
$Gap_{t-1}$	0.10	0.22	0.13
	(0.09)	(0.09)	(0.10)
$Gap_{t-2}$	0.03	0.03	-0.03
	(0.10)	(0.09)	(0.11)
$Gap_{t-3}$	0.10	-0.11	0.03
	(0.10)	(0.09)	(0.12)
$Gap_{t-4}$	-0.07	0.06	0.01
	(0.08)	(0.07)	(0.09)
$\Delta$ Rel Import Prices <sub>t</sub>	0.10	0.07	-0.23
	(0.04)	(0.04)	(0.05)
$\Delta$ Rel Import Prices <sub>t-1</sub>	-0.002 (0.04)	0.08 (0.04)	0.11 (0.05)
$\Delta$ Rel Import Prices <sub>t-2</sub>	0.04 (0.04)	-0.03 (0.05)	0.01 (0.05)
$\Delta$ Rel Import Prices <sub>t-3</sub>	-0.06 (0.04)	0.04 (0.04)	0.09 (0.05)
$\Delta$ Rel Import Prices <sub>t-4</sub>	0.03	-0.01	0.02
A D-1 E-1 & E-1	(0.04)	(0.04)	(0.05)
$\Delta$ Rel Fu & Energy Frices <sub>t</sub>	3.20	2.14	(0.22)
A Pol Ed & Energy Prices	(0.21)	(0.16)	(0.22)
$\Delta$ Ket Fu $\alpha$ Energy Thes <sub>t-1</sub>	(0.21)	(0.13)	(0.23)
$\Delta$ Rel Fd & Energy Prices <sub>t-2</sub>	-0.07 (0.21)	0.01 (0.32)	0.20 (0.22)
$\Delta$ Rel Fd & Energy Prices <sub>t-3</sub>	0.32 (0.21)	-0.21 (0.19)	0.03 (0.33)
$\Delta$ Rel Fd & Energy Prices <sub>t-4</sub>	-0.18	0.30	0.41
	(0.21)	(0.18)	(0.22)
NIXON_ON	-0.36	-0.31	-1.51
NIXON OFF	3.37	(1.08)	(0.90) 2.46
	(1.16)	(0.73)	0.71
Log Likelihood	-290.16	-249.08	-277.11
Standard Error of the Estimate	0.40	0.47	0.66

## Table 4: Time-varying Intercept Regressions with Time-varying NAIRU and breakin the Variance of the Intercept in 1967, 1984 and 1994

	CPI	PCE	GDP
Standard Deviation of Intercept 53-66	0.96	0.39	0.54
	(0.15)	(0.10)	(0.15)
Standard Deviation of Intercept 67-83	1.92	1.04	0.74
	(0.19)	(0.15)	(0.21)
Standard Deviation of Intercept 84-93	0.35	0.24	0.22
	(0.07)	(0.08)	(0.08)
Standard Deviation of Intercept 94-05	0.18	0.14	0.13
	(0.06)	(0.06)	(0.07)
NAIRU Gap <sub>t</sub>	0.20	0.21	-0.08
	(0.23)	(0.19)	(0.19)
NAIRU Gap <sub>t-1</sub>	-1.24	-0.91	-0.01
NAIRU Gap <sub>t-2</sub>	(0.25)	0.04 (0.28)	-0.22 (0.36)
NAIRU Gap <sub>t-3</sub>	-0.61	0.72	0.58
	(0.34)	(0.29)	(0.37)
<i>NAIRU</i> $Gap_{t-4}$	0.13	-0.47	-0.44
	(0.23)	(0.19)	(0.23)
$\Delta$ Rel Import Prices <sub>t</sub>	0.11	0.06	-0.24
	(0.04)	(0.04)	(0.05)
$\Delta$ Rel Import Prices <sub>t-1</sub>	0.001	0.10	0.13
	(0.04)	(0.04)	(0.04)
$\Delta$ Rel Import Prices <sub>t-2</sub>	0.06	-0.05	0.01
	(0.04)	(0.04)	(0.05)
$\Delta$ Rel Import Prices <sub>t-3</sub>	-0.07	0.03	0.10
	(0.04)	(0.04)	(0.05)
$\Delta$ Rel Import Prices <sub>t-4</sub>	0.01	-0.02	0.03
	(0.04)	(0.04)	(0.04)
$\Delta$ Rel Fd & Energy Prices <sub>t</sub>	3.34	2.06	1.36
	(0.21)	(0.18)	(0.22)
$\Delta$ Rel Fd & Energy Prices <sub>t-1</sub>	0.16	-0.13	0.13
	(0.20)	(0.18)	(0.23)
$\Delta$ Rel Fd & Energy Prices <sub>t-2</sub>	-0.21	-0.01	0.17
	(0.21)	(0.12)	(0.22)
$\Delta$ Rel Fd & Energy Prices <sub>t-3</sub>	0.29	-0.14	0.03
	(0.19)	(0.18)	(0.22)
$\Delta$ Rel Fd & Energy Prices <sub>t-4</sub>	-0.17	0.26	0.34
	(0.20)	(0.18)	(0.22)
NIXON_ON	-0.42	-0.25	-1.51
	(1.69)	(1.09)	(0.94)
NIXON_OFF	2.98	1.82	2.33
	(1.13)	(0.73)	(0.69)
Log Likelihood	-285.18	-241.45	-276.46
Standard Error of the Estimate	0.23	0.43	0.64

## Table 5: Time-varying Intercept Regressions with CBO Gap and break in theVariance of the Intercept at beginning of 1984 and Restrictions on Lags

	CPI	PCE	GDP
Standard Deviation of Intercept 64-83	1.42 <b>(</b> 0.15)	0.52 (0.11)	0.59 (0.16)
Standard Deviation of Intercept 84-03	0.23 (0.05)	0.18 (0.04)	0.16 (0.05)
$Gap_t$			
$Gap_{t-1}$	0.04	-0.01	-0.05
$Gap_{t-2}$	0.08	-0.04	0.08
$Gap_{t-3}$	-0.04 (0.12)	-0.17 (0.10)	-0.04 (0.11)
$Gap_{t-4}$	-0.02 (0.10)	0.25 (0.08)	0.04 (0.09)
$\Delta$ Rel Import Prices <sub>t</sub>			-0.26 (0.05)
$\Delta$ Rel Import Prices <sub>t-1</sub>	0.02 (0.05)	0.11 (0.04)	0.10 (0.05)
$\Delta$ Rel Import Prices	-0.01 (0.05) 0.02	-0.01 (0.04)	0.05 (0.05)
$\Delta$ Rel Import Prices <sub>1-4</sub>	-0.02 (0.04) 0.01	(0.04) 0.01	(0.08 (0.05) 0.04
$\Delta$ Rel Fd & Energy Prices <sub>t</sub>	(0.05) 5.64	(0.04) 3.78	(0.05) 2.40
$\Delta$ Rel Fd & Energy Prices <sub>t-1</sub>	(0.29) 0.26 (0.36)	(0.27) 0.24 (0.33)	(0.37) 0.32 (0.40)
$\Delta$ Rel Fd & Energy Prices <sub>t-2</sub>	0.07 (0.38)	0.08 .32	-0.11 (0.40)
$\Delta$ Rel Fd & Energy Prices <sub>t-3</sub>	0.36 (0.34)	0.08 (0.32)	0.18 (0.37)
$\Delta$ Rel Fd & Energy Prices <sub>t-4</sub>	0.04 (0.45) -0.63	0.73 (0.33) -0.88	0.45 (0.39)
NIXON_OFF	-0.03 (1.37) 3.40 (0.91)	-0.88 (0.72) 2.01 (0.54)	(0.83) 2.36 0.63
Log Likelihood Standard Error of the Estimate	-216.43 0.42	-181.58 0.54	-206.73 0.64



-5

1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004

----- Forward ----- Reverse

-0.6

1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004

## Figure 1 CPI Inflation Rate -- Gordon Equation

# Figure 2 PCE Inflation Rate -- Gordon Equation



-5

1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004

-0.6

1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004

---- Forward ---- Reverse



**Figure 3** GDP Inflation Rate -- Gordon Equation

Marginal R Squares of Recursive Regressions





-5.0

1964 1967 1970 1973

1976 1979 1982 1985 1988 1991 1994 1997 2000 2003

- INFCPI - RESID

-5.0

1964 1967 1970 1973 1976 1979 1982 1985 1988 1991 1994 1997 2000 2003

- INFCPI - LAGGAP

## Figure 5

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PCE Inflation: Gordon Equation: Sample Period 1964:2 - 2005:1



GDP Inflation: Gordon Equation: Sample Period 1964:2 - 2005:1

Figure 8

**One-Period Ahead Inflation Components** 





























One-Year Exante Real Treasury Rate



a) Real Rates: CPI Expected Inflation 10 8 6 4 2 0 -2 -4 -6 1956 1959 1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004 1953 3-Month Real Rate — One-year Real Rate — - Long-term Real Rate b) One-Year Real Rates PCE Expected Inflation 10.0 7.5 5.0 2.5 0.0 -2.5 -5.0 1953 1956 1959 1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004 - One-year Real Rate Long-term Real Rate 3-Month Real Rate 🗕 c) One-Year Real Rates GDP Expected Inflation 10.0 7.5 5.0 2.5 0.0 -2.5

Figure 17 Real Treasury Rate Term Structure

1953 1956 1959 1962 1965 1968 1971 1974 1977 1980 1983 1986 1989 1992 1995 1998 2001 2004

Long-term Real Rate

3-Month Real Rate — One-year Real Rate —

-5.0

