



# Concepts of Equilibrium Exchange Rates



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# What do we mean by Equilibrium?

- Existence, uniqueness, optimality, determination, evolution.....
- Can equilibrium be separated from the models?
- Importance of significance to question in hand

# Choosing how to measure equilibrium

- What time frame?
- What definition of the exchange rate?
- Modelling option
- Choosing between models

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# What time frame are we interested in?

- Short run
  - Market equilibrium
  - Current equilibrium
- Medium run
- Long run

# Modelling Exchange Rates

Dynamic path for exchange rate:

$$e_t = \beta' Z_t + \theta' T_t + \varepsilon_t$$

- Random disturbance
- Transitory factors
- Fundamentals

# What definition of the exchange rate?

- Real vs Nominal?
- Bilateral vs Effective?
- Choice of price index?

## Exchange rate measure (cont.)

- Terms of trade (price of exports compared to imports)
- Price of tradable goods or output prices
- Whole economy measures defined using
  - Consumer price indices
  - Unit labour costs
- Internal real exchange rate (tradables to non-tradables)

# Implementing an approach

- Modelling option
  - Model based
  - Estimation
- Choosing between models
  - Predictability
  - Co-movements
  - Long run



# Arbitrage based approaches

- Uncovered Interest Parity (UIP)
- Purchasing Power Parity (PPP)
- Balassa-Samuelson

**Empirical Justification?**

## UIP (in real terms)

$$e_t = E_t e_{t+1} + r_t - r_t^* + \sigma_t$$

Using forward substitution you get:

$$e_{t+k} - E_t e_{t+k} = \sum_{j=k}^{n-1} (E_{t+k} \delta_{t+j} - E_t \delta_{t+j}) + \sum_{j=k}^{n-1} (E_{t+k} \sigma_{t+j} - E_t \sigma_{t+j}) + (E_{t+k} e_{t+n} - E_t e_{t+n})$$

## Empirical justification?

# Do equilibrium exchange rates vary?

- Surely arbitrage should equalise prices?

i.e. purchasing power parity (PPP) and the law of one price (LOOP) should hold

Not necessarily:

## Continued.....

- Suppose LOOP holds. PPP may fail because
  - Different consumer preferences
  - Not all goods are traded
  - Produce different goods
- LOOP may also fail because
  - Transportation costs
  - Market structure (pricing to market)

**Empirical justification?**

# Balassa-Samuelson

- PPP for traded goods
- Labour mobile across sectors
- Productivity differentials between traded and non-traded sectors

$$e_t = (s_t + p_t^T - p_t^{T*}) - \alpha(p_t^T - p_t^{NT}) + \alpha^*(p_t^{T*} - p_t^{NT*})$$

**Empirical justification?**

# Short run models

- Monetary models
- Capital Enhanced Equilibrium Exchange Rates (CHEERs)
- Intermediate-term model-based EERs (ITMEERs)
- Behavioural Equilibrium Exchange Rates (BEERs)

**Empirical justification?**

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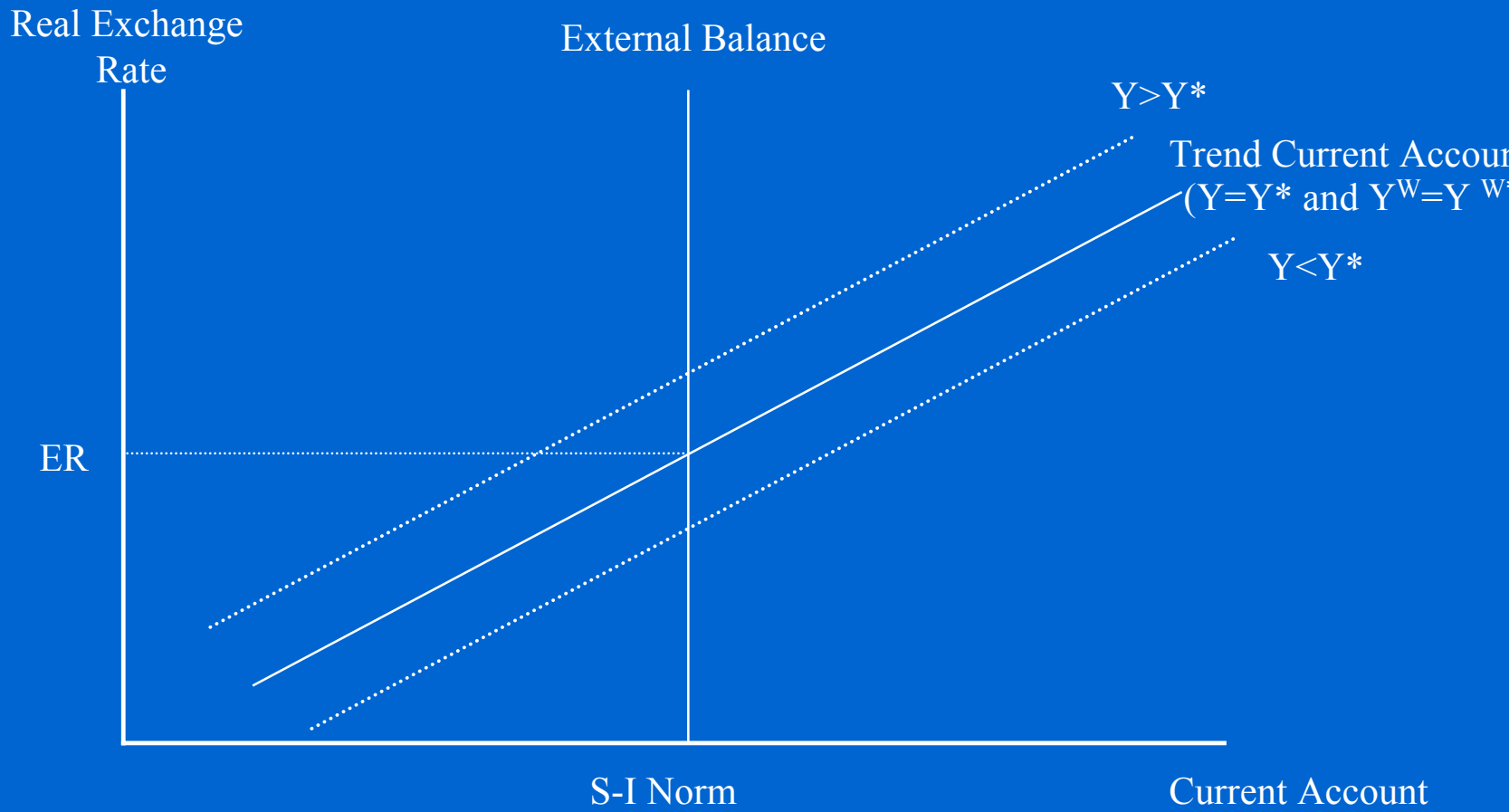
# Underlying Balance Models: The Medium Run

Internal and external balance

- Fundamental Equilibrium Exchange Rates (FEERs)
- Desired Equilibrium Exchange Rates (DEERs)

**Empirical justification?**

Fig 1: Stylised Model of the Underlying Balance model





# A simple economy:

Output supplied:

$$y_t^S = \bar{y}(A, K, \bar{L})_t$$

Output demanded:

$$y_t^D = DD_t + NT_t$$

Balance of Payments Identity:

$$CA_t = NT_t + BIPD_t = \Delta NFA_t = (S - I)_t$$

## Longer run measures

- Permanent Equilibrium Exchange Rates (PEERs)
- Atheoretical Permanent Eers (APEERs)
- Natural Real Exchange Rate (Natrex)

**Empirical justification?**

# Understanding the role of shocks

- Structural Vector Autoregressions (SVARs)
- Dynamic Stochastic General Equilibrium Models (DGSE)

**Empirical justification?**

# Table 1: Summary of Empirical Approaches to Estimating Equilibrium Exchange Rates

|                                | UIP   | PPP                                | Balassa-Samuelson   | Monetary Models                                       | CHEERS  | ITMEERs  | BEERs  | FEERs  | DEERs  | APEERs  | PEERs  | NATREX   | SVARs   | DSGE  |
|--------------------------------|---|------------------------------------|---|---|---|--|--|--|--|---|--|--|---|---|
| <b>Name</b>                    | Uncovered Interest Parity   | Purchasing Power Parity            | Balassa-Samuelson   | Monetary and Portfolio balance models                 | Capital Enhanced Equilibrium Exchange Rates       | <b>Intermediate Term Model Based Equilibrium Exchange Rates</b>  | Behavioural Equilibrium Exchange Rates   | Fundamental Equilibrium Exchange Rates   | Desired Equilibrium Exchange Rates   | Atheoretical Permanent Equilibrium Exchange Rates | Permanent Equilibrium Exchange Rates         | Natural Real Exchange Rates  | Structural Vector Auto Regression   | Dynamic Stochastic General Equilibrium models   |
| <b>Theoretical Assumptions</b> | The expected change in the exchange rate determined by interest differentials | Constant Equilibrium Exchange Rate | PPP for tradable goods. Productivity differentials between traded and nontraded goods | PPP in long run (or short run) plus demand for money. | PPP plus nominal UIP without risk premia          | Nominal UIP including a risk premia plus expected future movements in real exchange rates determined by fundamentals | Real UIP with a risk premia and/or expected future movements in real exchange rates determined by fundamentals | Real exchange rate compatible with both internal and external balance. Flow not full stock equilibrium | As with FEERs, but the definition of external balance based on <i>optimal</i> policy | None  | As BEERs                                     | As with FEERs, but with the assumption of portfolio balance (so domestic real interest rate is equal to the world rate). | Real exchange rate affected by supply and demand (but not nominal) shocks in the long run | Models designed to explore movements in real and/or nominal exchange rates in response to shocks. |
| <b>Relevant Time Horizon</b>   | Short run   | Long run                           | Long run  | Short run   | Short run (forecast)                              | Short run (forecast)   | Short run (also forecast)  | Medium run   | Medium Run   | Medium / Long run                                 | Medium / Long run                            | Long run   | Short (and long) run  | Short and long run  |
| <b>Statistical Assumptions</b> | Stationarity (of change)  | Stationary                         | Non-stationary  | Non-stationary  | Stationary, with emphasis on speed of convergence | None   | Non-stationary   | Non-stationary   | Non-stationary   | Non-stationary (extract permanent component)      | Non-stationary (extract permanent component) | Non-stationary   | As with theoretical   | As with theoretical   |
| <b>Dependent Variable</b>      | Expected change in the real or nominal  | Real or nominal                    | Real  | Nominal   | Nominal   | Future change in the Nominal   | Real   | Real Effective   | Real Effective   | Real  | Real   | Real   | Change in the Real  | Change relative to long run steady state  |
| <b>Estimation Method</b>       | Direct  | Test for stationarity              | Direct  | Direct  | Direct  | Direct   | Direct   | Underlying Balance   | Underlying Balance   | Direct  | Direct                                       | Direct   | Direct  | Simulation  |

# Modelling Accession countries

What features do we want?

- Traded v nontraded goods?
- Pricing to market?
  - In which direction?
- Risk premium?

Will depend on the question

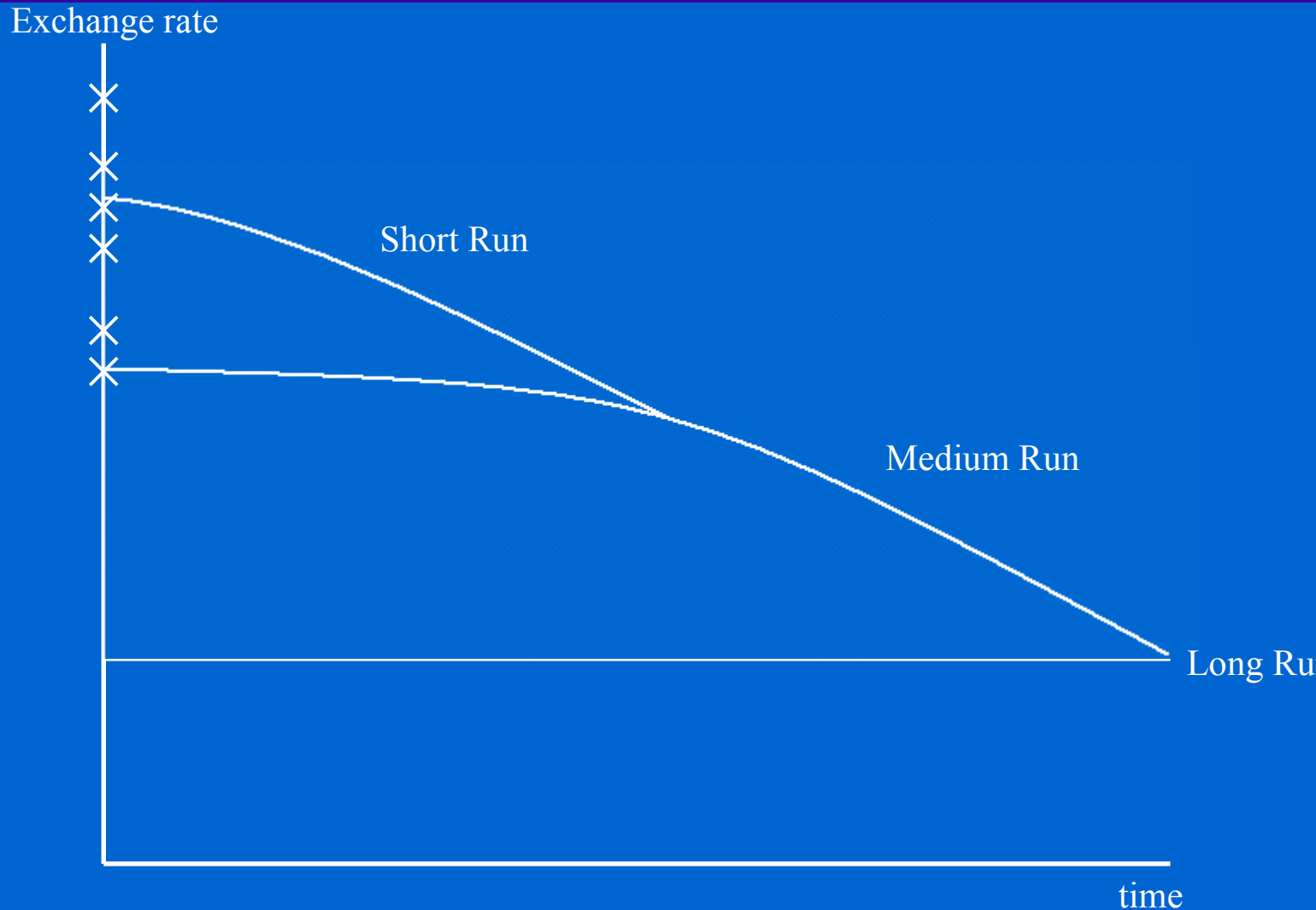
# Choosing an entry rate for EMU

- Actual exchange rate = short run equilibrium = medium run equilibrium = long run equilibrium
- Life is simple!!!!
  - With a small caveat about bilateral v effective exchange rates
- Sadly life is rarely simple!

# Exchange rates when shocks occur

- The exchange rate as a shock absorber v source of noise
- Good reasons why short, medium and long run equilibria differ
- Important to understand why

# Different time horizons





## Entry rates when shocks occur

- Entry rate = medium run  $\neq$  short run rate
  - Inflationary consequences
- Costs determined by:
  - reason why actual  $\neq$  medium run equilibrium
  - speed of adjustment to FEER outside EMU
- Choice of entry date important

# References

Westaway (2003) “Modelling the transition to EMU”, HM Treasury.

[http://www.hm-treasury.gov.uk/documents/the\\_euro/assessment/studies/euro\\_assess03\\_studwiltshire.cfm](http://www.hm-treasury.gov.uk/documents/the_euro/assessment/studies/euro_assess03_studwiltshire.cfm)

# Conclusions

- Remember the question of interest
- Models may have equal analytical status
- What will be important is their significance for task